### PixelCNN Models with Auxiliary Variables for Natural Image Modeling

**Alexander Kolesnikov**, IST Austria (joint work with Christoph Lampert) The Third Christmas Colloquium on Computer Vision, Moscow, Russia

#### Introduction

q(X) - true probability density over natural image  $X \in \mathcal{X}$ .  $X = \{x_1, \dots, x_n\}$  - collection of n pixels;  $x_i \in \{0, \dots, 255\}$  $D = \{X_1, X_2, \dots, X_m\}$  - i.i.d. samples from q.

**Goal**: use *D* to estimate probability density  $p(X) = p(x_1, ..., x_n)$ , which is close to *q*.

p(X) is also called *likelihood of X*.

- $p(X) \ge 0$
- $\sum_{X\in\mathcal{X}} p(X) = 1$
- Min.  $\operatorname{KL}(q||p) \Leftrightarrow \operatorname{Max.} \quad \underset{X \sim q}{\mathbb{E}} \log p(X) \approx \frac{1}{n} \sum_{X \in D} \log p(X)$

#### Motivation: image manipulations



Automatic colorization



#### Image debluring

- X' corrupted image
- $X^* = \underset{X \in \mathcal{X}}{\operatorname{argmax}} p(X) + \operatorname{similarity}(X, X').$

#### Motivation: reinforcement learning

#### Count-Based Exploration with Neural Density Models by Ostrovskiy et al.





#### Motivation: Defense against Adversarial Samples

PixelDefend: Leveraging Generative Models to Understand and Defend against Adversarial Examples by Song et al.





Category: wi-fi router

#### Motivation: generalization to other domains



Image modeling techniques generalize beyond images:

- Audio [Oord, Dieleman, et al. 2016]
- Video [Kalchbrenner et al. 2016]
- Natural language [Gulrajani et al. 2017]

#### **Research landscape**

GANs: Generative Adversarial Networks

• Implicit likelihood. Learns generator  $G: \mathcal{Z} \to \mathcal{X}$ 

VAEs: Variational AutoEncoders

• Intractable latent variable model:  $p(X) = \int_z p(X|z)p(z)dz$ 

#### Tractable models

• Explicit and computationally tractable likelihood p(X)

#### **Research landscape**

GANs: Generative Adversarial Networks

• Implicit likelihood. Learns generator  $G: \mathcal{Z} \to \mathcal{X}$ 

VAEs: Variational AutoEncoders

• Intractable latent variable model:  $p(X) = \int_{z} p(X|z)p(z)dz$ 

#### Tractable models

Explicit and computationally tractable likelihood p(X)
Autoregressive model + conv. network = PixelCNN

This ta

Main result

Introduce autoregressive models with auxiliary variables:

- Improved perceptual quality of produced samples.
- Improved sampling speed.

### Background: PixelCNN model

[Oord el al, ICML 2016] [Oord el al, NIPS 2016]

#### Key modeling idea: elementary chain rule

Represent a distribution over natural images as a product of one-dimensional conditional distributions:

$$p(X) = p(x_1, x_2, ..., x_n) = \prod_{i=1}^n p(x_i | x_1, ..., x_{i-1})$$

- Need to model only 1-dimensional distributions!
- Images are translation invariant, thus all conditional distributions can be modeled by a single function
- All conditional distributions can be computed in a single forward pass of an appropriate convolutional network

#### **PixelCNN** model



An illustration of how a single conditional distribution is computed.

Image credit: Conditional Image Generation with PixelCNN Decoders by Oord et al.

#### PixelCNN: implementation details



- Displaced receptive field
- Gatinig non-linearity:  $\phi(x) = \tanh(x_l) * \sigma(x_r)$

Straightforward to derive conditional model: p(X|z)

Image credit: Conditional Image Generation with PixelCNN Decoders by Oord et al.

$$D = \{X_1, X_2, \dots, X_m\}$$
 – training data

w - model parameters

#### Training procedure

Log-likelihood maximization using stochastic gradient descent:

$$\max_{w} \frac{1}{m} \sum_{X \in D} \sum_{i=1}^{n} \log p_{w}(x_{i}|x_{1}, \ldots, x_{i-1})$$

Gradients can be computed in a single backward pass

Sampling is sequential:  $x_1 \sim p(x_1)$   $x_2 \sim p(x_2|x_1)$   $x_3 \sim p(x_3|x_2, x_1)$   $x_4 \sim p(x_4|x_3, x_2, x_1)$ ...

Image credit: https://github.com/PrajitR/fast-pixel-cnn

#### Shortcomings of the PixelCNN model

• Lack of global structure in image samples:



• Slow sampling: deep neural networks needs to be invoked for every pixel which is being generated.

# PixelCNN models with Auxiliary Variables (ICML 2017)

We extend PixelCNN with auxiliary variable,  $\hat{X}$  and model a **joint** probability distribution:

$$p(X,\widehat{X}) = p(X|\widehat{X})p(\widehat{X})$$

Crucial modeling assumption:

 $\widehat{X} = f(X)$ , where f is a deterministic function.

In this talk:  $\widehat{X} = f(X)$  is an image, also modeled by PixelCNN. Efficient training: max  $\sum_{X \in D} [\log p(f(X)) + \log p(X|f(X))]$ Efficient sampling: sample  $\widehat{X}$  from  $p(\widehat{X})$ , then X from  $p(X|\widehat{X})$ 

#### Grayscale PixelCNN

Problem: Lack of global structure in random image samples

**Solution**: Explicitly encourage model to capture global image statistics

 $\widehat{X}$  – 4-bit quantized grayscale view of X

4-bit grayscale

original





 $\widehat{X}$  retains global image information and omits distracting texture patterns

#### Grayscale PixelCNN: insight into image modeling problem

Average loss of the trained model:

$$-\log p(\widehat{X}) pprox \mathbf{0.46} \qquad -\log p(X|\widehat{X}) pprox 2.52$$

Likelihood objective is dominated by colors/texture patterns



4-bit grayscale image transform is sufficient to produce photo-realistic images

#### Grayscale PixelCNN: samples



Grayscale PixelCNN samples are globally coherent.

#### Grayscale PixelCNN: likelihood

Model	Bits per dim.
Deep Diffusion [Sohl-Dickstein et al. 2015]	$\leq$ 5.40
NICE [Dinh, Krueger, and Y. Bengio 2014]	4.48
DRAW [Gregor, Danihelka, et al. 2015]	$\leq$ 4.13
Deep GMMs [Oord and Schrauwen 2014]	4.00
Conv Draw [Gregor, Besse, et al. 2016]	$\leq$ 3.58
Real NVP [Dinh, Sohl-Dickstein, and S. Bengio 2016]	3.49
Matnet + AR [Bachman 2016]	$\leq$ 3.24
PixelCNN [Oord, Kalchbrenner, and Kavukcuoglu 2016]	3.14
VAE with IAF [Kingma, Salimans, and Welling 2016]	$\leq$ 3.11
Gated PixelCNN [Oord, Kalchbrenner, Espeholt, et al. 2016]	3.03
PixelRNN [Oord, Kalchbrenner, and Kavukcuoglu 2016]	3.00
Grayscale PixelCNN [this talk]	$\leq 2.98$
DenseNet VLAE [Chen et al. 2017]	$\leq 2.95$
PixelCNN++ [Salimans et al. 2017]	2.92

The negative log-likelihood of the different models for the CIFAR-10 **test set** measured as bits-per-dimension.

#### Pyramid PixelCNN

Problem: Slow sampling

Solution: Multiscale decomposition

 $\widehat{X}$  – a low-resolution view of X. Can be applied recursively.

Start from generating tiny 8x8 seed Upscale 4 times to 128x128

Image generation = super-resolution

Tiny network for each step: 3 residual blocks  $\implies$  fast sampling



#### Pyramid PixelCNN

Problem: Slow sampling

Solution: Multiscale decomposition

 $\widehat{X}$  – a low-resolution view of X. Can be applied recursively.

Start from generating tiny 8x8 seed Upscale 4 times to 128x128

Image generation = super-resolution

Tiny network for each step: 3 residual blocks  $\implies$  fast sampling

Concurrent work: Parallel autoregressive density estimation Imporoves complexity by Reed et al:  $\mathcal{O}(n) \rightarrow \mathcal{O}(\log n)$ 



#### Pyramid PixelCNN: samples





Despite tiny PixelCNN models, which are used, high-resolution samples are accurate and globally coherent samples.

- High-frequency texture patterns dominate the likelihood objective
- Auxiliary quantized grayscale variable can be used to encourage PixelCNN model to focus more on semantic structure of an image
- Low-resolution auxiliary variables help to scale PixelCNN for high-resolution images
- Grayscale and low-resolution auxiliary variables can be combined

## Application: Probabilistic Image Colorization

Joint work with Amèlie Royer and Christoph Lampert (BMVC 2017)

#### **PixelCNN** for Automatic Colorization



#### Model: $p(X^{color}|X^{gray})$

- Handles diversity and pixel correlations
- Clean objective, no ad-hoc heuristics

Parallel work: PixColor: Pixel Recursive Colorization by Sergio Guadarrama et al

#### **Qualitative Results**



### Thank you for your attention!

Face generation demo: https://github.com/kolesman/FaceGeneration

> lmage colorization code: https://github.com/ameroyer/PIC

Apply for PhD at IST Austria: https://phd.pages.ist.ac.at/ Deadline: 8 January (very soon!)